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S/020/60/135/006/006/037  
C 111/ C 333

Asymptotic Expansions of Solutions to Ordinary Linear Differential Equations Having Small Coefficients With Their Higher Derivatives in the Neighborhood of an Irregular Singular Point

$$\lim_{\varrho \rightarrow 0} \psi_k(\varrho, \delta_0) = \psi_k(\delta_0) = \begin{cases} \psi_k^0 & \text{if } 2 \leq k \leq m \\ \psi_k^0 - \delta_0 & \text{if } m+1 \leq k \leq n \end{cases}$$

Let  $\psi_0 \leq \psi_k(\delta_0) \leq \psi_0 + 2\pi$ . Let

$$(13) \quad 1.) \quad z \in G_k(\varrho, \delta_0) \quad \text{if} \quad -2/3\pi - \psi_k(\varrho, \delta_0) < \arg z <$$

$$< 2/3\pi - \psi_k(\varrho, \delta_0)$$

$$2.) \quad z \in G_k(\delta_0), \quad \text{if} \quad -2/3\pi - \psi_k(\delta_0) < \arg z < 2/3\pi$$

$$- \psi_k(\delta_0)$$

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3.)  $z \in G_k^0$ , if  $-2/3\pi - \psi_k^0 < \arg z < 2/3\pi - \psi_k^0$ .

Let  $G_0$  be the intersection of the  $G_k^0$ ;  $G(\delta_0)$  intersection of the  $G_k(\delta_0)$ ;  $G(\zeta, \delta_0)$  intersection of the  $G_k(\zeta, \delta_0)$ . Let  $G_\alpha(\delta_0)$  be narrower than  $G(\delta_0)$  and let it be contained in  $G(\zeta, \delta_0)$  for all sufficiently small  $\zeta$ . By the transformation

$$(14) W(z, \varepsilon) = e^{\lambda_1(\varepsilon)z} \tilde{G}_1(\varepsilon) u(z, \varepsilon)$$

let (1) pass over into

$$(15) L[u; \varepsilon] = \sum_{k=m+1}^n \varepsilon^{k-m} p_k(z, \varepsilon) u^{(k)} + \sum_{k=0}^m p_k(z, \varepsilon) u^{(k)} = 0,$$

where

$$p_n(z, \varepsilon) = 1, p_k(z, \varepsilon) = \sum_{s=0}^{\infty} \varepsilon^s a_{k,s}(z) = \sum_{s=0}^{\infty} z^{-s} b_{k,s}(\varepsilon).$$

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Let  $L[u, \varepsilon]$  be represented as

$$(23) \quad \bar{L}[u, \varepsilon] = \sum_{s=0}^{\infty} \varepsilon^s \bar{L}_s[u]$$

where

$$\bar{L}_0[u] = u^{(m)} + \sum_{k=0}^{m-1} a_{k,0}(z) u^{(k)}, \quad \bar{L}_s[u] = \sum_{k=m+1}^n a_{k,s-k+m}(z) u^{(k)} + \sum_{k=0}^{m-1} a_{k,s}(z) u^{(k)}, \quad \text{where } a_{k,s} = 0 \text{ for } s < 0.$$

Theorem: Let  $u(z, \varepsilon)$  be the solution of (15) and have the asymptotic expansion

$$(28) \quad u(z, \varepsilon) \simeq 1 + \sum_{s=1}^{\infty} c_{1,s}(\varepsilon) z^{-s} \text{ in } G_{\alpha}(\delta_0).$$

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Assume that the function  $u_0(z)$  satisfies

$$(25) \quad \bar{L} [u_0] = 0$$

and has the asymptotic expansion

$$(27) \quad u_0(z) \simeq U_1(z) = 1 + \sum_{s=1}^{\infty} c_{1,s}^0 z^{-s} \text{ in } G_0,$$

while the functions  $u_s(z)$  are determined by the equations

$$(26) \quad \bar{L}_0 [u_s] = - \sum_{\mu=0}^{s-1} \bar{I}_{\mu} [u_{s-1-\mu}]$$

as well as by the condition that they decrease at infinity as  $1/z$  in  $G_0$ . Then the formal expansion of  $u(z, \varepsilon)$  in terms of  $\varepsilon$ -powers

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$$(24) \quad U(z, \varepsilon) = \sum_{s=0}^{\infty} \varepsilon^s u_s(z)$$

is asymptotic in  $G_{\alpha}(\delta_0)$  for  $\varepsilon \rightarrow 0$  ( $\arg \varepsilon = \delta_0$ ) so that

$$\lim_{\varepsilon \rightarrow 0} u(z, \varepsilon) = u_c(z) .$$

The author thanks Yu. L. Rabinovich and D. P. Kostomarov for assistance.

There are 6 references: 5 Soviet and 1 Belgian.

ASSOCIATION: Moskovskiy gosudarstvennyy universitet imeni M. V. Lomonosova (Moscow State University imeni M. V. Lomonosov)

PRESENTED: July 7, 1960, by J. G. Petrovskiy, Academician

SUBMITTED: July 7, 1960

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28811

S/140/61/000/005/007/007  
0111/0222

16.3300

AUTHOR: Khapayev, M. P.

TITLE: The asymptotic development of hypergeometric and degenerated hypergeometric functions

PERIODICAL: Izvestiya vysshikh uchebnykh zavedeniy. Matematika, no. 5, 1961, 98-101

TEXT: The author obtains asymptotic developments of the hypergeometric function  $F(a, b, c, z)$  and the degenerated hypergeometric function  $F(a, c, z)$  for the case that  $a$  and  $c$  are large and have the same order. The author starts from the equations

$$z \frac{d^2 u}{dz^2} - (z-c) \frac{du}{dz} - au = 0 \quad (1)$$

and

$$z(1-z) \frac{d^2 u}{dz^2} + [c - (a+b+1)z] \frac{du}{dz} - abu = 0 \quad (13)$$

respectively, where  $a = \alpha l$ ,  $c = \gamma l$ ,  $l \rightarrow \infty$ ,  $\alpha \neq 0$ ,  $\gamma \neq 0$ ,  $h$

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S/140/61/000/005/007/007  
G111/0222

The asymptotic development . . .

introduces the new variable  $t = \frac{\alpha}{\gamma} z$  and obtains equations with a small parameter for the highest derivative, e. g. (1) changes in

$$\varepsilon t v'' + [\varepsilon t(d+1) + \gamma] v' + \varepsilon t d v = 0 \quad (2)$$

with  $v(t) = e^{-t} u(\frac{\gamma}{\alpha} t)$ ;  $d=1 - \frac{\gamma}{\alpha}$ ;  $\varepsilon = \frac{1}{\alpha}$ . The asymptotic development of the solution of (2) regular in 0 corresponds to  $F(a, b, z)$ .

Thus the author obtains the developments

$$F(\alpha, \gamma, z) \approx e^{\frac{\alpha}{\gamma} z} \left\{ 1 + \frac{1}{1} \frac{\left(\frac{\alpha}{\gamma}\right)^2}{2} \left(\frac{1}{\alpha} - \frac{1}{\gamma}\right) + \frac{1}{1^2} (\dots) + \dots \right\}$$

and

$$F(a, b, c, z) = u(t) \approx \dots \quad \} \quad (17)$$

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The asymptotic development . . .

$$\simeq (1-t)^{-b} \left\{ 1 + \varepsilon \frac{b(b+1)}{2} \left( \frac{1}{y} - \frac{1}{x} \right) \frac{1-2t}{(1-t)^2} + \varepsilon^2(\dots) + \dots \right\}. \quad (17)$$

For large  $m, n$  and  $\left| \frac{m-n}{m+n} \right| \ll 1$  from (17) it follows a new asymptotic development for the adjoint Legendre functions:

$$\begin{aligned} P_n^m(x) &= \frac{\Gamma(m+n)}{2^m \Gamma(m) \Gamma(n-m)} (x^2-1)^{\frac{m}{2}} F\left(m-n; n+m+1; m+1; \frac{1-x}{2}\right) \simeq \\ &\simeq \frac{\Gamma(m+n)}{2^m \Gamma(m) \Gamma(n-m)} (x^2-1)^{\frac{m}{2}} \left(1 - \frac{n+m+1}{m+1} \frac{1-x}{2}\right)^{n-m} \times \\ &\times \left\{ 1 + \frac{(m-n)(m-n+1)n}{2(m+1)(m+n+1)} \cdot \frac{1 - \frac{n+m+1}{m+1} \frac{(1-x)}{2}}{\left(1 - \frac{n+m+1}{m+1} \frac{1-x}{2}\right)^2} + \dots \right\}. \end{aligned}$$

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C111/C222

The asymptotic development . . .

The author thanks Yu. L. Rabinovich for the attention for the paper.  
There are 2 Soviet-bloc and 1 non-Soviet-bloc references.

ASSOCIATION: Moskovskiy gosudarstvennyy universitet imeni M. V.  
Lomonosova (Moscow State University imeni M.V.Lomonosov)

SUBMITTED: March 28, 1959

Card 4/4

S/042/61/C16/004/004/005  
C111/C444

AUTHOR: Khapayev, M. M.

TITLE: Linear differential equations with small coefficients  
at some of the highest order derivatives in the  
neighborhood of an inessential singular point

PERIODICAL: Uspekhi matematicheskikh nauk, v.16, no. 4, 1961,  
187-194

TEXT: The following equation is considered

$$\bar{\mathcal{L}}[u] = \sum_{k=1}^{\mu} \varepsilon^k z^{m+k} \bar{p}_{m+k}(z, \varepsilon) \frac{d^{m+k} u}{dz^{m+k}} + \sum_{h=0}^m z^h \bar{p}_h(z, \varepsilon) \frac{d^h u}{dz^h} = 0 \quad (1)$$

where  $\bar{p}_l(z, \varepsilon)$  are analytic with  $z$  and  $\varepsilon$  in the neighborhood of the  
point  $(0,0)$ ,  $\bar{p}_{m+\mu}(0,0) \neq 0$  and  $\bar{p}_m(0,0) \neq 0$ . The point  $z = 0$  is an  
inessential singular point of (1). The coefficients  $\varepsilon^k z^{m+k} \bar{p}_{m+k}(z, \varepsilon)$   
have a zero of at least  $k^{\text{th}}$  order for  $z = 0$  with respect to  $\varepsilon$ , if  
 $1 \leq k \leq \mu - 1$ , and a zero of  $k^{\text{th}}$  order, if  $k = \mu$ . The defining

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Linear differential equations with . . . S/042/61/016/004/004/005  
C111/C444

equation for the characteristic exponents  $\varrho$  of the point  $z = 0$  is

$$\sum_{k=1}^{\infty} \varrho(\varrho-1)\dots(\varrho-m-k+1)\varepsilon^k \bar{p}_{m+k}(0,\varepsilon) + \sum_{h=0}^m \varrho(\varrho-1)\dots(\varrho-h+1) \bar{p}_h(0,\varepsilon) = 0 \quad (2)$$

For  $\varepsilon \rightarrow 0$   $\mu$  roots of (2) go to infinity and  $m$  roots pass continuously over into the roots of the defining equation

$$\sum_{h=0}^m \varrho(\varrho-1)\dots(\varrho-h+1) \bar{p}_h(0,0) = 0 \quad (3)$$

of the degenerate differential equation. Let  $\varrho_1$  be a simple root of (3) and  $\varrho_1(\varepsilon)$  be a root of (2), where  $\varrho_1(0) = \varrho_1$  and (2) do not possess any roots  $\varrho_1(\varepsilon) + 1$ ,  $1 > 0$  being an integer.

If one puts  $u(z, \varepsilon) = z^{\varrho_1(\varepsilon)} w(z, \varepsilon)$ , then  $w(z, \varepsilon)$  satisfies the equation

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C111/C444

$$\mathcal{L}[w] = \sum_{k=1}^{\infty} \varepsilon^k z^{m+k-1} p_{m+k}(z, \varepsilon) w^{(m+k)} + \sum_{h=1}^m z^{h-1} p_h(z, \varepsilon) w^{(h)} + p_0(z, \varepsilon) w = Q(5)$$

This equation possesses a regular solution for  $\varepsilon = 0$  which can be searched formally in the form

$$\bar{w}(z, \varepsilon) = \sum_{i=0}^{\infty} \varepsilon^i w_i(z) \quad (9)$$

$w_i(z)$  are determined by recurrent relations after putting (9) in (5) and by the initial conditions

$$w_0(0) = 1, w_{h+1}(0) = 0 \quad (h = 0, 1, 2, \dots) \quad (11)$$

The author proves that the formal expansion (9) is the asymptotic expansion of the regular solution of (5) in a domain G. The domain G consists of the  $\varepsilon$  - plane, out of which certain angular domains are cut;  $z$  must satisfy the condition  $|z| < R_2$  where a certain upper

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Linear differential equations with . . . S/042/'61/016/004/004/005  
C111/0444

bound is given for  $R_2$ .

A. N. Tikhonov, A. B. Vasil'yeva, J. S. Gradshteyn are mentioned; the author thanks Yu. L. Rabinovich for useful advices.

There are 4 Soviet-bloc references and 1 non-Soviet-bloc reference.

SUBMITTED: August 17, 1959

Card 4/4

5/039/62/057/002/002/003  
B172/B112

AUTHOR: Khapayev, M. M. (Moscow)

TITLE: Asymptotic expansions in the neighborhood of an irregular pole of solutions of ordinary linear differential equations with small coefficient in the higher derivatives

PERIODICAL: Matematicheskiy sbornik, v. 57(99), no. 2, 1962, 187-200

TEXT: An equation

$$\sum_{k=m+1}^n \epsilon^{k-m} \bar{p}_k(z, \epsilon) w^{(k)} + \sum_{k=0}^m \bar{p}_k(z, \epsilon) w^{(k)} = 0$$

with  $p_n(z, \epsilon) = 1$ ,  $\lim_{\epsilon \rightarrow 0} p_m(z, 0) \neq 0$  is considered. The coefficients  $p_k$  are assumed to be analytic in the neighborhood of  $\epsilon = 0$ ,  $z = \infty$ . This point then is an irregular second-order pole. The formal solutions of the differential equation can be constructed as normal series. For each formal solution, a complete neighborhood of the point, at infinite distance, can be decomposed into a series of angular domains in such a way that, for

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KHAPAYEV, M.M. (Moskva)

Asymptotic behavior near an irregular singular point of solutions of ordinary linear differential equations with small coefficients at the higher derivatives, Mat. sbor. 57 no.2: 187-200 Ja '62. (MIRA 15:6)  
(Differential equations, Linear)

L 45457-65 EWA(m)/T/EWA(m)-2

ACCESSION NR: AP5009831

UR/0367/65/001/002/0274/0276

AUTHOR: Khapov, M. M.

TITLE: On the stability of motion of a charged particle in a magnetic field

SOURCE: Yadernaya fizika, v. 1, no. 2, 1965, 274-276

TOPIC TERMS: helical field, charged particle motion, magnetic focusing, strong focusing system, betatron oscillation, adiabatic invariant, particle accelerator

ABSTRACT: The general averaging methods developed by N. N. Bogolyubov and Yu. A. Mitropol'skiy (Asimptoticheskiye metody v teorii nelineynykh kolebaniy [Asymptotic Methods in the Theory of Nonlinear Oscillations], Fizmatgiz, 1963) and by V. M. Volosov (UMN v. 17, 3, 1962) are used to investigate the motion of a charged particle in a straight helical field. Such an investigation is of interest in connection with strong focusing systems of magnetic lenses for high-energy particles. Adiabatic invariants of the averaged system are constructed and it is shown that the particle can be trapped in the vicinity of the helical-symmetry axis of the field. The resultant equations can be linearized for small betatron oscillations near an equilibrium position, and the frequency of the small oscillations can be

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determined. The results show that the averaged trajectories and the solution of the system remain close to one another over a finite number of slow cycles. Orig. art. has: 6 formulas.

ASSOCIATION: Moskovskiy gosudarstvennyy universitet (Moscow State University).

SUBMITTED: 25/10/64

ENCL: 00

SUB CODE: KP

NR REF SOV: 003

OTHER: 000

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L 63004-6 EWT(m)/EPA(w)-2/EWA(m)-2 Pt-7 IJ(c)  
 ACCESSION NO: AF5016527

UR/0188/65/003/003/1057/0063  
 530.12:531.51

AUTHOR: Klapayev, M. M. (Member of mathematics dept)

TITLE: On focusing of beams of high speed charged particles in stellerator type fields

SOURCE: Moscow. Universitet. Vestnik. Seriya 3. Fizika, astronomiya, no. 3, 1965, 57-63

TOPIC TAGS: charged particle, magnetic field, particle trajectory, high energy accelerator, trajectory equation

ABSTRACT: The focusing properties of a high energy beam of charged particles were studied analytically in a helical magnetic field. The components of the magnetic field are given by

$$\begin{aligned} H_r &= H_0 \left( \frac{r}{r_0} \right)^{m-1} \sin m(\varphi - \alpha_2), \\ H_\varphi &= H_0 \left( \frac{r}{r_0} \right)^{m-1} \cos m(\varphi - \alpha_2), \\ H_z &= -H_0 \left( \frac{r}{r_0} \right)^m \alpha \cos m(\varphi - \alpha_2), \end{aligned}$$

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and the particle trajectory equations are written in cylindrical coordinates  $r, \varphi, z$ , under the assumption that  $v/v_0 \ll 1$ . Two more equations are given of the type

$$\ddot{r} - r\dot{\varphi}^2 = \frac{ev}{cm} \cdot \frac{H_0}{r_0^{m-1}} (-1)^{m-1} \cos m(\varphi - \omega t),$$

$$r\ddot{\varphi} + 2\dot{r}\dot{\varphi} = \frac{ev}{cm} \cdot \frac{H_0}{r_0^{m-1}} r^{m-1} \sin m(\varphi - \omega t),$$

$$z = v_0 t, \quad \omega = \omega_0,$$

called longitudinally unperturbed equations. It is further assumed that the frequency  $\omega$  is very small or  $|\frac{\dot{\varphi}}{\omega}| \ll 1$  and the following small quantity is

introduced  $\frac{1}{(mv)^2} = \epsilon$ ,  $\psi = \varphi - \omega t$ . The final form of the trajectory equations is then given by the set of equations

$$u = -b \cos \theta,$$

$$\theta = 1 + \frac{b}{u} \sin \theta + \epsilon(m-1) \frac{u}{r} \sin(\theta - \psi),$$

$$\dot{\psi} = 1 + \epsilon m \frac{u}{r} \sin(\theta - \psi),$$

$$r = eu \cos(\theta - \psi).$$

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ACCESSION NO: AP5016627

where  $\psi = m(\varphi + \omega t)$ . The solution of these equations is obtained by means of a simplified degenerate system of equations with two adiabatic invariant integrals

$$p + 2a^2 r^{2(n-1)} = \text{constant} = A,$$

$$(\lambda - \beta^2)^{n-1} \beta^2 s^{2(n-1)} \Phi = \gamma,$$

which describes a periodic motion for the average system. This in turn permits certain conclusions to be made about the focusing capabilities of such charged particle beams. It is shown that interactions between transverse motion and longitudinal motion in the beam are very small. The author expresses his gratitude to A. N. Tikhonov for his very valuable comments on the results. Orig. art. has: 25 equations.

ASSOCIATION: Moskovskiy gosudarstvennyy universitet, Kafedra matematiki (Moscow State University, Department of Mathematics)

SUBMITTED: 15 Apr 64

ENCL: 00

SUB CODE: NP

NO REF SOV: 002

OTHER: 000

Card 3/3 *ilk*

L 5136-66 EWT(m)/EPA(w)-2/EWA(m)-2 IJP(c)  
ACCESSION NR: AP5018745

UR/0020/65/163/002/0343/0346

AUTHOR: Khapayev, M. M.

TITLE: Nonlinear theory of the motion of fast charged particles in helical toroidal magnetic fields

SOURCE: AN SSSR. Doklady, v. 161, no. 2, 1965, 343-346

TOPIC TAGS: charged particle, particle acceleration, helical magnetic field, focusing accelerator

ABSTRACT: The author considers helical fields rolled into a torus whose central diameter  $R$  is much larger than the cross section diameter  $\sigma_0$ ; the pitch  $L$  of the helical field is also assumed larger than  $\sigma_0$ . Such magnetic fields can be used for hard focusing of charged particles in accelerators and charged-particle guidance systems. An averaging method is used to construct adiabatic invariants, which describe nonlinear oscillations analogous to betatron oscillations. The equations describing these oscillations are linearized for small oscillation amplitudes, and formulas describing the main linear resonances of the system are obtained for their frequencies. The motion of the particle in such a field is considered both in the presence and in the absence of a turning field. Relations are obtained between the parameters of the system ( $R$ ,  $L$ ,  $\sigma_0$ ) and the intensities of the helical and turning

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ACCESSION NR: AP5018745

fields. Possible distortions of the system are discussed. This report was presented by M. A. Leontovich. Orig. art. has: 1 formulas.

ASSOCIATION: Moskovskiy gosudarstvennyy universitet im. M. V. Lomonosova (Moscow State University)

SUBMITTED: 22Dec64

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INCL: 00

(OTHER: 000

SUB CODE: NP

OC  
Card 2/2

I, 38430-66 EWT(1)/T IJP(c)

ACC NR: AP6025277

SOURCE CODE: UR/0188/66/000/003/0040/0046

AUTHOR: Khapayev, M. M.

ORG: Department of Mathematics, Moscow State University (Kafedra matematiki, Moskovskiy gosudarstvennyy universitet)

TITLE: Nonlinear motion theory of fast charged particles in helical toric magnetic fields

SOURCE: Moscow. Universitet. Vestnik. Seriya III. Fizika, astronomiya, no. 3, 1966, 40-46

TOPIC TAGS: ~~force field, polar coordinates, potential equation~~, Bessel function, harmonic oscillation, *particle motion, fast particle, charged particle, helical magnetic field*

ABSTRACT: Helical force fields are analysed. These fields are bent into tori with a chosen radius  $R$  which is greater than the radius  $a$  of the toric cross section. The motion in this field occurs on a helix whose pitch  $L$  is greater than the radius of the toric cross section. A particle moves in the toric field under the action of an upturning force and without it. The motion is analyzed by polar coordinates on the plane of the toric cross section. The potential equation is expressed by the toric parameters and the Bessel function of complex arguments which can be expanded into series. Equations for the components of the helical field with an upturning field were developed. A fast particle, moving along the axis of the helical field, can be considered to be under the action of a rapidly rotating force. This force causes

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ACC NR: AP6025277

a systematic drift of the particle. Introducing integral parameters as variable arguments, the particle motion can be analyzed on the cross-section plane of the torus. The particle moves slowly on a circumference on the cross-section plane, making two slight harmonic oscillations on the circumference. The same particle participates in the rapid motion of the field. Orig. art. has: 22 formulas. [EG]

SUB CODE: 20/ SUBM DATE: 15Dec64/ ORIG REF: 005/ ATD PRZSS: 5043

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I. 06324-67 FWT(d) IJP(c)

SOURCE CODE: UR/0376/66/002/005/0600/0608

ACC NR: AP6017447

AUTHOR: Khapavev, M. M.

ORG: Moscow State University im. M. V. Lomorosov (Moskovskiy gosudarstvennyy universitet)

TITLE: Method of averaging and several problems connected with averaging

SOURCE: Differentsial'nyye uravneniya, v. 2, no. 5, 1966, 600-608

TOPIC TAGS: ordinary differential equation, approximation method

ABSTRACT: A proof is given of N. N. Bogolyubov's averaging principle, which is based on the direct comparison of solutions of the input and averaged systems under general assumptions about the right-hand member. The object of study is systems of ordinary differential equations describing the motion of charged particles in special magnetic fields. For the system

$$\frac{dx}{dt} = \varepsilon X(t, x) \quad (1)$$

the following theorem is proved: Let a function  $X(t, x)$  be defined for  $t > 0$  and  $x$  belonging to a region  $D$ , and let the following conditions be fulfilled: a)  $X(t, x)$  satisfies Karateodori's conditions, which assure the existence of a continuous solution  $x(t)$ ; b) there exists a summable function  $W(t)$  and a constant  $N_0$  such that for  $t \geq 0$

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and  $t \geq 0$  and  $x \in D$   $|X(t, x)| \leq N(t)$ , and for any finite interval  $[t_1, t_2]$  the following holds

$$\int_{t_1}^{t_2} N(t) dt \leq V_0(t_2 - t_1);$$

c) there exists a summable function  $H(t)$  and a constant  $H_0$ , and also a non-vanishing function  $\psi(\alpha)$ ,  $\lim_{\alpha \rightarrow 0} \psi(\alpha) = 0$ , such that for  $t > 0$  and  $x \in D$

$$|X(t, x') - X(t, x'')| \leq \psi(|x' - x''|) H(t), \quad \int_{t_1}^{t_2} H(t) dt \leq H_0(t_2 - t_1)$$

on any finite interval  $[t_1, t_2]$ ; d) there exists a limit in  $D$  uniform relative to  $x$

$$\lim_{T \rightarrow \infty} \frac{1}{T} \int_0^T X(t, x) dt = X_0(x);$$

e)  $X_0(x)$  in region  $D$  satisfies the Lipschitz condition

$$|X_0(x') - X_0(x'')| \leq \lambda |x' - x''|.$$

Then with any  $\eta > 0$ , however small, and with any large  $L$  one may associate a quantity  $\epsilon_0$  such that if  $\xi = \xi(t)$  is a solution of the averaged system

$$\frac{d\xi}{dt} = \epsilon X_0(\xi),$$

defined in the interval  $0 < t < \infty$  and lying in region  $D$  along with its  $\eta$ -neighborhood,

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then for  $0 < \varepsilon < \varepsilon_0$  in the interval  $0 < t < \frac{L}{\varepsilon}$  the following inequality holds

$$|x(t) - \xi(t)| < \eta,$$

in which  $x(t)$  is a solution of system (1) coinciding with  $\xi(t)$  when  $t = 0$ . The author thanks A. N. Tikhonov, B. M. Budak, and V. M. Volosov for their useful comments. Orig. art. has: 45 formulas.

SUB CODE: 12/

SUBM DATE: 14Jun65/

ORIG REF: 010/

OTH REF: 002

Card 3/3 *hde*

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UDC: 517.9:533.9

ACC NR: AT6034338

This, in turn, yields the characteristic equation for the cyclotron frequency  $\nu$ . The particle motion is then analyzed for small values of the parameter  $\varepsilon$ , and it is shown that the adiabatic invariants  $\lambda$  and  $\gamma$ , given by

$$\dot{p}^2(\eta + s_0) = \lambda, \quad \frac{\lambda^2}{p^2} + p^2(s_0^2 + \frac{1}{2} + p^2) = \gamma,$$

describe a slow, nonlinear oscillation for the particle motion. Orig. art. has: 22 equations.

SUB CODE: 20/ SUBM DATE: 28Jan65/ ORIG REF: 009

Card 2/2

AUTHOR: Khapayev, P.V., Engineer SOV-91-58-4-6/29

TITLE: On the Article of S.S. Gadzhiyev "On the Increase of the Number of Consumer Lines Connected with One Common Switch of 6 and 10 kv" (Po povodu stat'i S.S. Gadzhiyeva "Ob uvelichenii chisla potrebitel'skikh liniy, podklyuchayemykh pod odin vyklyuchatel' 6 i 10 kv")

PERIODICAL: Energetik, 1958, Nr 4, p 7, (USSR)

ABSTRACT: The author questions statement of S.S. Gadzhiyev that economy of an installation can be obtained by an increase of the number of consumer lines connected with one common switch of 6 and 10 kv. None of the circuits illustrating his article is justified by practical need. On the contrary, the reliability of the consumer's power supply is lowered.

1. Switching systems--Effectiveness

Card 1/1

KHAPAYEV, V.M., inzh.

Behavior of sodium sulfite as additive to boiler feed water.

Trudy RIIZHT no.46:4-27 '63.

(MIRA 18:1)

KHAPAYEV, V.M., inzh.

Behavior of sodium sulfite when used as an additive in boiler water.  
Teploenergetika 11 no. 1:49-52 Ja '64. (MIRA 17:5)

1. Rostovskiy institut inzhenerov zheleznodorozhnogo transporta.

KHAPAYEV, V.M., inzh.; KUBANOV, A.T., inzh.

Wash-off of silicic acid deposits in the sulfitation of boiler  
feedwater. Trudy RIIZHT no.46:28-35 '63. (MIRA 18:1)

KVAKIN, S.D., inzh.; KUBANOV, A.T., inzh.; KHAPAYEV, V.M., inzh.

Steam corrosion of steel used in the manufacture of boiler turbines  
in the presence of the products of decomposition of sodium sulfite.  
'Trudy RIIZHT no.46:36-41 '63. (MIRA 18:1)



KHAPAYEVA, A.K., inzh.

Interuniversity conference devoted to the 22nd Congress of  
the CPSU. Izv. vjs. ucheb. zav.; energ. 4 no.8:123-125  
Ag '61. (MIRA 14:8)

1. Leningradskiy politekhnicheskiy institut im. M.I.  
Kalinina.

(Hydraulic engineering)  
(Electric power plants)

KHAPAZHEV T. Sh.

USSR/Pharmacology, Toxicology - Narcotics.

U-1

Abs Jour **APPROVED FOR RELEASE: 09/17/2001** **CIA-RDP86-00513R000721810002**

Author : Shautsukova, L.K., Khkhashonov, N.I., Khapazhev, T.Sh.,  
Khakulov, L.A., Dzohlayev, A.A.

Inst : -

Title : Certain Physiologic and Biochemical Changes in Rabbits  
During Amytal-Induced Sleep.

Orig Pub : Uch. Zap. Kabardinsk. gos. ped. in-t, 1956, vyp. 10, 113-  
126.

Abstract : Experiments were performed on male rabbits. A 15% solu-  
tion of sodium amytal in a dose of 1.5-2 ml. was adminis-  
tered into the ear vein on 3 successive days. During  
the amytal-induced sleep, total plasma proteins decreased  
in proportion to the duration of the sleep. Blood sugar  
and iron decreased during the first two days but then be-  
gan to increase until the sleep was terminated. During  
the amytal-induced sleep there was a decrease in Hb. and

Card 1/2

USSR/Pharmacology, Toxicology - Narcotics.

U-1

Abs Jour : Ref Zhur - Biol., No 3, 1958, 12845

KHAPAZHEV, T.Sh.

Thresholds of the formation and the characteristics of local responses  
of the surface of the cerebral cortex evoked by direct electric  
stimulation under the influence of stimulants and narcotics. Vest.  
LGU 18 no.9:115-131 '63. (MIRA 16:6)  
(STIMULANTS) (ELECTROENCEPHALOGRAPHY) (NARCOTICS)

KHAPAZHEV, T. Sh.

Eff. of barbiturates on the excitability and electric activity  
of the cerebral cortex. Nerv. sist. no. 4:138-139 '63  
(MIRA 18:1)

1. Fiziologicheskii Institut Leningradskogo Universiteta.

BARADULINA, Mariya Georgiyevna; KHAPERIYA, R.V., red.; PRONINA,  
N.D., tekhn. red.

[Clinical aspects and treatment of regional metastases in  
laryngeal cancer] Klinika i lechenie regional'nykh metasta-  
zov raka gortani. Moskva, Medgiz, 1963. 166 p.

(MIRA 16:10)

(LARYNX—CANCER) (METASTASIS)

30963. KHAPILIN, A. G., MOISEYEV, S. G., AND SOKOLOVA, V. P.

Iechenie penitsillinom v klinike vnutrennikh bolezney. V sb: Voprosy  
ostroy vnutrenney kliniki. M., 1949, s. 247-58

21012

S/058/61/000/005/020/050

A001/A101

24.6600

AUTHORS:

Morozova, P.V., Tleubergenova, G.A., Khapilin, V.N.

TITLE:

Interaction of 660-Mev protons with nuclei of light and heavy elements of the photoemulsion.

PERIODICAL:

Referativnyy zhurnal. Fizika, no 5, 1961, 99-100, abstract 5B433  
("Uch. zap. Alma-Atinsk. gos. ped. in-t, 1958, (1959), v 12, no 2, 172-187)

TEXT:

Stars produced by 660-Mev protons in nuclei of light (C, N and O) and heavy (Ag and Br) elements were studied with the aid of  $\text{HUK}\Phi\text{M}$  (NIKFI) photoemulsion. The total effective cross section was determined for inelastic interactions of protons with nuclei of the emulsion. Differential cross sections agree with that calculated on the basis of the optical nucleus model. Recoil protons formed in light nuclei possess higher energies than protons from heavy nuclei. The study of angular distribution of cascade particles has shown the preferential forward directional flux in light nuclei.

[Abstracter's note: Complete translation.]

Card 1/1

IL'IN, K.P., kand. tekhn. nauk; KHAFILOV, Yu.A., kand. tekhn. nauk;  
SHESTAKOV, Yu.K., inzh.

Specialization of gondola cars is an efficient measure.  
Zhel. dor. transp. 47 no. 11:22-26 N '65 (MIRA 1981)

KHAPILOV, Yu. A.

"Choosing a Rational Method and the Fundamental Parameters of the Heating of a Railroad Car." Cand Tech Sci, Moscow Order of Lenin, and Labor Red Banner Inst of Railroad Transport Engineers named I. V. Stalin, Min Railways USSR, Moscow, 1954. (KL, No 1, Jan 55)

Survey of Scientific and Technical Dissertations Defended at USSR Higher Educational Institutions. (13)

SC: Sum. No. 598, 29 Jul 55



KHAPILOV, Yu.A., kand. tekhn. nauk; TALALAY, V.I., inzh.

Design and calculation of the curve-in ability of coupled cars.  
Vest. TSNII MPS 25 no.1:31-34 '66. (MIRA 19:2)

KHAPILOV, Yu., mladshiy nauchnyy sotrudnik; ZHURILOV, V., mladshiy nauchnyy sotrudnik

Use by foreign countries of plastics and synthetic materials in shipbuilding (from "Quarterly Transactions of the Institute of the Institute of Naval Architecture," no.3, July 1958). Mor.flot 19 no.8: 38-40 Ag '59. (MIRA 12:11)

1. Institut kompleknykh transportnykh problem AN SSSR.  
(Shipbuilding) (Plastics)

ACC NR: AP7003257

(N)

SOURCE CODE: UR/0207/66/000/006/0096/0097

AUTHOR: Khapilova, N. S. (Novosibirsk)

ORG: none

TITLE: Axisymmetrical flow in a thin layer of fluid on the surface of a revolving body of revolution

SOURCE: Zhurnal prikladnoy mekhaniki i tekhnicheskoy fiziki, no. 6, 1966, 96-97

TOPIC TAGS: Body of revolution, fluid flow, boundary flow, axisymmetric flow

ABSTRACT: This paper examines a problem earlier proposed by the author in which a system of equations was derived which describes flow in a fluid layer on the surface of a revolving body of revolution in a nonstationary system of coordinates associated with the body. Only axisymmetrical flow is studied. An analysis of theoretical data shows that in calculating nonsteady axisymmetric flow in a tube of finite length two boundary conditions must be given on the left and one on the right if the flow is "precritical," i.e.,  $v_1 < \sqrt{fh}$ , or three boundary conditions on the left if flow is "supercritical," i.e.,  $v_1 > \sqrt{fh}$ . When specifically choosing the boundary conditions in the case of steady axisymmetric flow it is of interest to study the possible forms of the free surface. The author introduces the concept of critical depth into the equations studied to determine the pre- or supercriticality of flow conditions. At

Card 1/2

ACC NR: AP7003257

greater than critical depths flow is such that depth continuously decreases; at less than critical depths flow is such that depth continuously increases. There are three forms of free surface in the first case and two in the second. Orig. art. has: 16 formulas.

SUB CODE: 20/ SUBM DATE: 06Aug65/ ORIG REF: 002

Card 2/2

VASILYEV, O.F.; KHAPILOVA, N.S. (Novosibirsk)

"An analysis of axisymmetric swirling inviscid flow in bounded regions"

report presented at the 2nd All-Union Congress on Theoretical and Applied Mechanics, Moscow, 29 January - 5 February 1964



L 29047-00 ENT(1)/EWP(m)/ENT(m)/T IJP(c) DS/NW/DJ

ACC NR: AP6013205

SOURCE CODE: UR/0421/66/000/002/0102/0107

AUTHOR: Nikitin, A. K. (Rostov-na-Donu); Khapilova, V. S.  
(Rostov-na-Donu)

ORG: none

TITLE: The nonlinear problem of a spherical suspension

SOURCE: AN SSSR. Izvestiya. Mekhanika zhidkosti i gaza, no. 2, 1966, 102-107

TOPIC TAGS: nonlinear theory, viscous flow

ABSTRACT: The article treats the problem of the steady state motion of an incompressible viscous fluid between two concentric spheres. Into the gap between the spheres fluid is fed in through one opening, and through another opening it is withdrawn. The two concentric spheres are designated  $A_1$  and  $A_2$ , and their radii as  $r_1$  and  $r_2$  ( $r_1 < r_2$ ). In sphere  $A_2$  there are two diametrically opposed openings: opening  $S_1$ , through which fluid is fed, and opening  $S_2$ , through which it is withdrawn. Assuming the motion of the fluid to be axisymmetric and neglecting mass forces, the equations of motion can be written as follows in a spherical system of coordinates:

Card 1/2

L. 29849-66

ACC NR: AP6013205

$$\begin{aligned} \frac{\partial}{\partial r} \left( \frac{v_r^2 + v_\theta^2}{2} \right) - \frac{D\psi}{r^2 \sin^2 \theta} \frac{\partial \psi}{\partial r} + \frac{1}{p} \frac{\partial p}{\partial r} &= \frac{v}{r^2 \sin^2 \theta} \frac{\partial D\psi}{\partial \theta} \\ \frac{\partial}{\partial \theta} \left( \frac{v_r^2 + v_\theta^2}{2} \right) - \frac{D\psi}{r^2 \sin^2 \theta} \frac{\partial \psi}{\partial \theta} + \frac{1}{p} \frac{\partial p}{\partial \theta} &= -\frac{v}{\sin \theta} \frac{\partial D\psi}{\partial r} \\ (D = \frac{\partial^2}{\partial r^2} + \frac{\sin \theta}{r^2} \frac{\partial}{\partial \theta} \left( \frac{1}{\sin \theta} \frac{\partial}{\partial \theta} \right), v_r = \frac{1}{r^2 \sin \theta} \frac{\partial \psi}{\partial \theta}, v_\theta = -\frac{1}{r \sin \theta} \frac{\partial \psi}{\partial r}) \end{aligned} \quad (1.1)$$

Here D is the Stokes operator;  $\psi$  is the flow function;  $v_r, v_\theta$  are components of the velocity. The article is devoted to a mathematical solution of the above problem. Orig. art. has: 11 formulas.

SUB CODE: 20/ SUBM DATE: 27Aug65/ ORIG REF: 003/ OTH REF: 001

Card 2/2 f/

BENSMAN, V.M., kand.med.nauk (Krasnodar, ul.Gogolya, d.65, kv.11)  
MIRPIL, B.M.; MISEREV, V.S.

APPROVED FOR RELEASE: 09/17/2001

CIA-RDP86-00513R000721810002-

Concerning L.I.Shulutko's article "Posture defects and scoliosis." Ortop., travm. i protez. 26 no.12:78-79 D '65.  
(MIRA 19:1)

1. Iz kafedry gosptital'noy khirurgii (zav. - doktor med.nauk B.N.Esperov) Kubanskogo meditsinskogo instituta i Krasnodarskiy krayevoy klinicheskoy bol'nitsy (glavnyy vrach - zasluzhennyy vrach RSFSR G.V.Novitskaya). Submitted June 3, 1965.



MEAPKINA, V.V.; PILATSKIY, P.O.

Automatic machine for assembling cardan axle crosspieces. Avt.prom.  
no.11:37-38 N '60. (MIRA 13:11)

1. Moskovskiy zavod malolitrzhnykh avtomobiley i Nauchno-issledovatel'skiy institut tekhnologii avtomobil'noy promyshlennosti.  
(Machine-shop practice)

IVANOV, S.N.; KHAPKINA, Z.A.

Effect of various methods of introducing the superphosphate and  
humus mixture on the assimilation of phosphorus by corn. Dokl.  
AN BSSR 7 no.7:485-487 J1 '63. (MIRA 16:10)

1. Belorusskiy nauchno-issledovatel'skiy institut pochvovedeniya  
Ministerstva sel'skogo khozyaystva BSSR.

KHAPKINOV, A., agronom po zashchite rasteniy

Disinfecting and loading machine. Zashch. rast. ot vred. 1 bol. 9  
no.9:25 '64. (MIRA 17:11)

KHAPKO, V. U.

Khapko, V. U.

"The Problem of Applying Hardening Processes to the Hub Portions of Railroad-Car Axles." Min Railways USSR. Moscow Order of Lenin and Order of Labor Red Banner Inst of Railroad Transport Engineers Ireni I. V. Stalin. Moscow, 1955 (Dissertation for the degree of Candidate of Technical Sciences)

SO: Knizhnaya letopis' No. 27, 2 July 1955

*KHAPKO, V.U.*

ZOBININ, N.P., doktor tekhn. nauk, prof.; ROGOV, A.Ya., kand. tekhn. nauk, dots.;  
KHAPKO, V.U., assistant.

Strengthening wheel pair axles by rolling. Trudy MIIT no.93:3-72  
'57. (MIRA 11:4)  
(Car axles) (Rolling (Metalwork))

ZOBNIN, N.P., doktor tekhn. nauk, prof., KHAPKO, V.U., kand. tekhn.  
nauk, dotsent

Hardening treatment of axles after prolonged operation. Trudy  
MIIT no.159:30-52 '62. (MIRA 16:6)

(Car axles—Maintenance and repair)  
(Metals—Cold working)

ZOBNIN, N.P., doktor tekhn. nauk, prof.; ROGOV, A.Ya., kand. tekhn.  
nauk, dotsent; KHAFKO, V.U., kand. tekhn. nauk, dotsent;  
YUDIN, D.L., kand. tekhn. nauk, dotsent

Effect of the cold working depth on the service life of axle  
press joints. Trudy MIIT no.159:89-98 "62. (MIRA 16:6)

(Car axles)

(Metals—Cold working)

ZOBNIN, N.P., doktor tekhn.nauk, prof.; KHAPKO, V.U., kand.tekhn.nauk, dotsent

Increasing the efficiency of the cutting of gear wheels for locomotive transmissions. Trudy MIIT no.200:5-20 '54.

Mechanical hardening of gear wheels with the relieved surface of a worm cutter on the gear cutting machine. Ibid.:47-53

(MIRA 18:8)



<sup>11</sup>  
G M KHAPLANOV

"Interchangeability of Tubes in Radio Engineering Apparatus" from  
Annotations of Works Completed in 1955 at the State Union Sci. Res. Inst. Min.  
of Radio Engineering Ind.

Sc: B-2,080,964

В. Н. Курин  
Статистические методы анализа в статистической радиофизике.

11 июня  
(с 16 до 22 часов)

М. С. Александров  
Распределение параметров фазовых и амплитудных флуктуаций сигнала, шума и корреляционных функций сигнала.

В. С. Фадеев  
История теории построения и теории информации для дискретных каналов с шумом.

О. С. Шапова  
Определение вероятности потерь в системах с помехами и шумами.

Р. Р. Воронцов  
История развития теории кодирования информации.

12 июня  
(с 10 до 16 часов)

М. Н. Бабкин  
Системы передачи информации по каналам с фазовыми помехами.

М. М. Ткаченко  
Оптимальный приемник сигнала с шумом и помехами.

Г. Н. Рунцов,  
Г. М. Емельянов  
Системы передачи информации.

Г. Н. Рунцов,  
Г. М. Емельянов  
О построении оптимальных систем приема и передачи информации в каналах с шумом и помехами.

А. А. Сачко  
История развития теории построения и теории информации для дискретных каналов с шумом.

13 июня  
(с 16 до 22 часов)

В. Н. Марченко  
Групповые передачи информации с шумом и помехами.

А. А. Емельянов  
Вопросы оптимального построения систем приема и передачи информации.

report submitted for the Confidential Meeting of the Scientific Technological Society of  
Radio Engineering and Electrical Communications in. A. G. Popov (YEMEN), Moscow,  
5-12 June, 1959

В. Л. Кривор  
Прогноз для неаэрозольных технологий про-  
грамм на основе новых систем

12 часов  
(с 10 до 16 часов)

М. Н. Прохоров  
Измерение фазовых характеристик в телекоммуникациях

А. Л. Лавин  
О применении фазовых методов в телекоммуникациях и в радиотехнике

С. Д. Руднев  
Перспективы применения фототехники для радиотехники

М. Г. Давыдов  
Прибор для измерения мощности телекоммуникационного сигнала

12 часов  
(с 10 до 16 часов)

В. В. Кривор  
Телекоммуникационные технологии в радиотехнике

30

Ч. Г. Постриж  
Телекоммуникационные системы, использующие широкую полосу

М. Н. Кривор  
Устройства для автоматизации приборов

В. В. Кривор

М. Г. Давыдов

О применении фазовых методов в телекоммуникациях и в радиотехнике

# 1. СЕКЦИЯ ЭЛЕКТРОНИКИ

Президент, М. Д. Давыдов

9 часов  
(с 10 до 16 часов)

Г. М. Руднев

С. Д. Руднев

Новые методы радиотехники и в радиотехнике

В. А. Афанасьев

Перспективы применения фототехники в радиотехнике

30

report submitted for the Confidential Meeting of the Scientific Technological Society of  
Radio Engineering and Electrical Communications in A. S. Popov (VKSIE), Moscow,  
5-12 June, 1959

KHAPLANOV, M. G.

O kharaktere stepennykh razlozheniy funktsiy, imeyushchikh na krugе skhodimosti odnu osobuyu tochku. Rostov N/D, Uchen. Zap. Un-Ta., 8 (1936), 92-130.

SO: Mathematics in the USSR, 1917-1947  
edited by Jurosh, A. G.,  
Markushevich, A. L.,  
Rashevskiy, P. K.  
Moscow-Leningrad, 1948

KHAPLANOV, M. G.

O koeffitsiyentakh ryada teylora odnogo klassa meromorfnykh funktsiy. DAN,  
28 (1940), 679-684.

SO: Mathematics in the USSR, 1917-1947.  
edited by Jurosh, A. G.,  
Markushevich, A. L.  
Rashevskiy, P. K.  
Moscow-Leningrad, 1948

"On the Taylor Coefficients of a Class of Metomorphic Functions,"

Physico-Math. Inst., ~~Rostov State Univ~~ ~~Rostov State Univ~~ Rostov State Univ. in Molotov

1. 6624 M. I. Some properties of an analytic space  
Avt. Akad. Nauk SSSR (N 5: 70, 024-031, 1957)

The space is the set  $A_B(A_B)$  of all sequences  $x(x_1, x_2, \dots)$  of complex numbers such that  $f(t) = x_1 + ix_2 + \dots$  is an analytic function of the complex variable  $z$  for  $|z| < R$ . In the terminology of Köthe and Toeplitz [1]  $A_B(A_B)$  is a  $(\mathcal{L}, \mathcal{L})$ -space with  $\mathcal{L} = \mathcal{L}_1$  and  $\mathcal{L}_2 = \mathcal{L}_2$  (see Köthe [2], p. 171; [3], 226; [4], § 4; Köthe [5], p. 108; [6], p. 108; [7], p. 12; [8], p. 12) the norm  $\|x\|_B = \sup_{|z| < R} |f(z)|$ ,  $\|x\|_{A_B} = \|x\|_B$ ,  $\|x\|_{A_B}^* = \|x\|_B$ ,  $\|x\|_{A_B}^{**} = \|x\|_B$  so that  $A_B(A_B)$  is a  $(\mathcal{L}, \mathcal{L})$ -space (see [9], p. 12).  $M(A_B)$  is bounded if and only if the corresponding set of functions has a majorant in  $A_B(A_B)$ .

4.  $M(A)$  is an ergent sequence in the Köthe sense  $\Leftrightarrow M(A)$  is bounded if and only if  $A$  is a Köthe sequence.

Letter to the Editor

7 : 13 N J

111

Mapla. ov. M Linear transformation

—DAG 35.

$\frac{d}{dt} \left( \frac{\partial L}{\partial \dot{x}} \right) = \frac{\partial L}{\partial x}$

the matrix of the transformation (for  $\Delta \neq 0$ ) is

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1951 - October 1952 - 14 352 N 111 T 3000 - 10000

1. *Chlorophyll a* and *Chlorophyll b* were determined by the method of Arar and Collins (1971) using a Shimadzu 1010 UV-Visible Spectrophotometer.

1. *Journal of the American Medical Association*, 1997; 277: 1039-1043.

...and the fact that the *Journal* is a journal of the American Psychological Association, the largest and most influential organization in the field of psychology, adds to the journal's prestige and makes it a must-read for all psychologists.

1. *Journal of the American Medical Association*, 1997; 278: 1039-1044.

<sup>a</sup>  $\chi^2$  test for independence.  $\chi^2 = 10.2$ ,  $df = 1$ ,  $p = 0.002$ .  
<sup>b</sup>  $\chi^2$  test for independence.  $\chi^2 = 10.2$ ,  $df = 1$ ,  $p = 0.002$ .

1. *Journal of the American Medical Association*, 2000; 283: 2686-2692.

4. It is not and only it is not.

8. *Journal of the American Statistical Association*, 93, 1998, 1039-1052.

Figure 1. The effect of the concentration of the polymer on the rate of polymerization.

*Journal of Management Education* 30(6)p.789-804

1. *Chlorophyll a* and *Chlorophyll b* were determined by the method of Lichtenthal and Whistler (1973).

$$b = 1.0 \pm 0.002$$

Figure 1. The effect of the initial concentration of the monomer on the polymerization of  $\alpha$ -methylstyrene initiated by  $\text{Zn}^{2+}$  in the presence of  $\text{Na}_2\text{S}_2\text{O}_8$  at  $30^\circ\text{C}$ . The reaction conditions were:  $[\text{Na}_2\text{S}_2\text{O}_8] = 0.005 \text{ mol/L}$ ,  $[\text{Zn}^{2+}] = 0.005 \text{ mol/L}$ ,  $[\text{M}] = 0.05 \text{ mol/L}$ ,  $[\text{H}_2\text{O}] = 0.55 \text{ mol/L}$ ,  $t = 10 \text{ min}$ .

Haplan, M. G. A. Malina  
of analytic functions.

60 51-180 (1961) R. 45.

A. 1961, 1962, 1963.

1964, 1965.

1966, 1967.

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KHAPLANOV, M. G.

Functional Analysis

Matrix sign of the completeness of a system of analytic functions. Dokl. AN SSSR 83  
No. 1 1952.

Moskovsky Gosudarstvenny Universitet: Im. V. M. Molotova Recd. 26 Oct. 1951.

SO: Monthly List of Russian Accessions, Library of Congress, August <sup>2</sup>195~~3~~, Uncl.

Mathematical Review.  
June 1954  
Analysis

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Molotov

① Haplanov, M. G. On the spectral theory of matrices in an analytic space. Doklady Akad. Nauk SSSR (N.S.) 90, 969-972 (1953). (Russian)

The principal theorem states that if  $f_n(x)$  is a sequence of functions analytic in  $|x| < R$ , with a matrix mapping the analytic space  $A_{R_1}$  into  $A_{R_2}$ ,  $R_1 < R$  [cf. Haplanov, same Doklady (N.S.) 80, 21-24, 177-180 (1951); these Rev. 13, 470, 357], then the sequence  $h_n(x) = x^n - \lambda f_n(x)$  is a quasi-power basis in  $|x| < R$  for any  $\lambda$  which is not an eigenvalue of the integral equation

$$\varphi(x) = f(x) + \lambda \int_C K(x, s) \varphi(s) ds,$$

where  $K(x, s) = (2\pi i)^{-1} \sum_{j=0}^{\infty} f_j(x) \overline{f_j(s)} / s^{j+1}$ , and  $C$  is any circle  $|x| = r < R$ . Similar problems relating to fundamental systems and normal bases in analytic spaces are reduced to problems about the spectra of integral equations.

B. Crabtree (Durham, N. H.).

KHAPLANOV, M. G.

UDC 517.512.6 - Matrices Eigenvalues 1 Sep 53

"Point Character of the Spectrum of a Certain Class of Matrices in Analytical Space," N. N. Rozhanskaya

DAN SSSR, Vol 92, No 1, pp 7-10

Considers an infinite matrix  $M(a_{jk})$  ( $j, k = 1, 2, \dots$ ) that transforms an analytic space  $A_R$  ( $0 < R < \infty$ ) into itself (M. G. Khaplanov, DAN, 86, Nos 1, 2 (1951)). Notes that M. G. Khaplanov was the first to study the character of the spectrum of such matrices (DAN, 90, No 6, 1953). Studies the spectrum by the method of converging sequences of matrices. Generalizes M. G. Khaplanov's conditions

274T61

for the presence of purely point spectrum (i. e. eigenvalues). Presented by Acad M. V. Keldysh  
30 Jun 53.

GAKHOV, F.D.; KHAPLANOV, M.G.; AL'PER, S.Ya.

"Brief outline of mathematical analysis." A.IA.Khinchin. Reviewed  
by F.D.Gakhov, M.G.Khaplanov, S.IA.Al'per. Usp.mat.nauk 9 no.4:  
266-275 '54. (MIRA 8:1)  
(Calculus) (Khinchin, Aleksandr Iakovlevich, 1894- )

Haplanov, M. V. Spectrum of a matrix in an analytic space. Rostov. Gos. Univ. Uč. Zap. Fiz.-Mat. Fak. 32 (1955), no. 4, 3-8. (Russian)

After mentioning a number of properties of the space  $l_1$  (all functions analytic in the unit circle) and  $l_\infty$  (all functions whose power series have bounded coefficients) the author proves that any matrix  $M$  mapping  $l_1$  into  $l_1$  has a point spectrum. That is, there exists a non-zero vector  $x$  such that  $Mx = \lambda x$ . The inverse  $M^{-1}$  exists if and only if  $\lambda \neq 0$ . The author also proves that the set of all finite limit points of the spectrum of  $M$  is a closed set. The theory of integral equations is also mentioned.

116  
Hilb, M. L. Linear differential equations of infinite  
order with analytic coefficients. Dokl. Akad. Nauk  
SSSR 105 (1955) 1167-1168.

It is made of the functions  
Borel-Leopitz coefficients  
the concept of the series  
and this matrix  $M$  are dependent in the  
homogeneous system of equations  $Af=0$  has a non-trivial  
solution  $f$  and the series  $f$  is

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HADLEROV, A. G.

(1) and associated matrices of the operator  $N$  is of class I if and only if the operator matrix

$$N = \begin{pmatrix} a_{00} & a_{01} & \dots \\ a_{10} & a_{11} & \dots \\ \vdots & \vdots & \ddots \end{pmatrix}$$

transforms space  $A_1$  into  $A_2$ . [Definition of these spaces appears in an earlier work of the author same Dokl. (N.S.) 79 (1951), 929-932; MR 13, 252.] 2. Let  $L[y]$  be of class I. If  $f(x) \in E_n$ , then equation (1) has a solution  $y \in E_n$  if and only if the vectors  $c, b$  satisfy the system  $Lc = b$ . (Here  $M = (a_{ij})$ , where  $a_{ij} = \sum_{n=0}^{\infty} (1/n!) a_{ij,n}$ ;  $c = (c_0, c_1, \dots)$ , where  $y(x) = \sum_{n=0}^{\infty} (c_n/n!) x^n$ ; and  $b = (b_0, b_1, \dots)$ .) An interesting application is made to the equation  $\sum_{n=0}^{\infty} (a_n + b_n x) y^{(n)} = f(x)$ .

I. M. Sheffer.

2/2

HAPLANOV, M. G.

Haplanov, M. G. Infinite matrices in an analytic space.  
Uspehi Mat. Nauk (N.S.) 11 (1956), no. 3(71), 37-44.  
(Russian)

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Let  $A_R$  and  $A_H$  denote the spaces of points  $x = (x_1, x_2, \dots)$  whose coordinates satisfy the conditions

$$\limsup |x_n|^{1/n} \leq 1/R, \quad \limsup |x_n|^{1/n} < 1/R,$$

respectively. The author indicates various ways in which such spaces can be interpreted as spaces of analytic functions. He also considers the continuous linear operators  $T$  which (collectively) map an infinite-dimensional vector space  $E$  into an infinite-dimensional vector space  $E_1$ . In order that  $T$  map  $A_R$  with  $R=1$  into itself, it is necessary and sufficient that (i) the columns of its matrix  $M = (a_{jn})$  have a common majorant belonging to  $A_1$  and (ii) there exist two constants  $q$  ( $0 < q < 1$ ) and  $m$  such that  $|a_{jn}| < q^n$  for  $n > mj$ . The author classifies the matrices  $M$  with regard to linear independence of rows and of columns, and interprets the classification in terms of the mappings  $T$ . For example, if the rows of  $M$  are linearly independent, while some of the columns are dependent, then either  $M$  has infinitely many left inverses, and  $T$  maps  $E$  on all of  $E_1$ ; or  $M$  has no inverses, and  $T$  maps  $E$  on a dense subset of  $E_1$ ; in both cases, infinitely many points of  $E$  are carried into one point.

The theory is applied to the problem of determining

whether a system  $\{f_n\}$  is a basis in  $A_1$ .

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Let  $\{x_n\}$  be a sequence of real numbers such that  $x_n \geq 0$  for all  $n$  and  $\sum_{n=1}^{\infty} x_n < \infty$ . Then  $\lim_{n \rightarrow \infty} x_n = 0$ .  
 Proof: Suppose  $\lim_{n \rightarrow \infty} x_n \neq 0$ . Then there exists a subsequence  $\{x_{n_k}\}$  such that  $\lim_{k \rightarrow \infty} x_{n_k} = L \neq 0$ . Since  $x_n \geq 0$ , we have  $L \geq 0$ . If  $L > 0$ , then for sufficiently large  $k$ ,  $x_{n_k} > L/2$ . This implies that  $\sum_{k=1}^{\infty} x_{n_k} = \infty$ , which contradicts the assumption that  $\sum_{n=1}^{\infty} x_n < \infty$ . Therefore,  $L = 0$ . Since every subsequence of  $\{x_n\}$  has a further subsequence that converges to 0, it follows that  $\lim_{n \rightarrow \infty} x_n = 0$ .  
 Corollary: If  $\{x_n\}$  is a sequence of real numbers such that  $x_n \geq 0$  for all  $n$  and  $\sum_{n=1}^{\infty} x_n < \infty$ , then  $\lim_{n \rightarrow \infty} x_n = 0$ .  
 Example: Let  $x_n = 1/n^2$ . Then  $\sum_{n=1}^{\infty} x_n = \sum_{n=1}^{\infty} 1/n^2 < \infty$ . By the corollary,  $\lim_{n \rightarrow \infty} 1/n^2 = 0$ .  
 Theorem: Let  $\{x_n\}$  be a sequence of real numbers. Then  $\lim_{n \rightarrow \infty} x_n = L$  if and only if for every  $\epsilon > 0$ , there exists a positive integer  $N$  such that  $|x_n - L| < \epsilon$  for all  $n \geq N$ .  
 Proof: Suppose  $\lim_{n \rightarrow \infty} x_n = L$ . Let  $\epsilon > 0$ . Then there exists a positive integer  $N$  such that  $|x_n - L| < \epsilon$  for all  $n \geq N$ . Conversely, suppose that for every  $\epsilon > 0$ , there exists a positive integer  $N$  such that  $|x_n - L| < \epsilon$  for all  $n \geq N$ . Let  $\epsilon = 1/k$  for  $k = 1, 2, 3, \dots$ . Then for each  $k$ , there exists a positive integer  $N_k$  such that  $|x_n - L| < 1/k$  for all  $n \geq N_k$ . Let  $n = \max\{N_1, N_2, \dots, N_k\}$ . Then  $|x_n - L| < 1/k$  for all  $k$ . This implies that  $\lim_{n \rightarrow \infty} x_n = L$ .

*Khaplanov, M.G.*

LITVINCHUK, G.S.; KHAPLANOV, M.G.

Bases and complete systems in the space of analytic functions of  
two variables. Usp.mat.nauk 12 no.4:319-325 J1-Ag '57. (MIRA 10:10)  
(Functions, Analytic) (Functions of several variables)  
(Matrices)

KHAPLANOV, Mikhail Grigor'yevich; ROZHANSKAYA, N.M., otv.red.;

SHKORINOV, V.P., red.; PAVLICHENKO, M.I., tekhn.red.

[Theory of functions of complex variables] Teoriia funktsii  
kompleksnogo peremennogo; kratkii kurs. Rostov-na-Donu, Izd-vo  
Rostovskogo univ., 1959. 193 p. (MIRA 14:2)  
(Functions of complex variables)

KHAPLANOV, M. G., Doc Phys-Math Sci -- (diss) "Linear operators in analytic space and their application." Khar'kov, 1960. 11 pp, (Ministry of Higher and Secondary Specialist Education, Ukrainian SSR, Khar'kov Order of Labor, Red Banner State Univ im A. M. Gor'kiy), 200 copies, free, bibliography at end of text (20 entries), (KL, 17-60, 138)

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S/044/60/000/009/006/021  
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AUTHOR: Khaplanov, M.G.

TITLE: Linear Operators in an Analytic Space

PERIODICAL: Referativnyy zhurnal. Matematika, 1960, No.9, pp.57-58,  
Abstract No.10209. Uch.zap.Fiz-matem.fak. Rostovsk. un-t,  
1959, Vol.43, No.6, pp.83-118

TEXT: The author considers spaces  $A_R (\bar{A}_R)$ ,  $0 < R < \infty$ , of all sequences  $x(x_0, x_1, \dots)$  the coordinates of which satisfy the condition

$\lim_{n \rightarrow \infty} \sqrt[n]{|x_n|} \leq \frac{1}{R} (\lim_{n \rightarrow \infty} \sqrt[n]{|x_n|} < \frac{1}{R}, R < \infty)$ . The topology in these spaces is

introduced according to the method of Köthe and Toeplitz (Köthe, G., Toeplitz, O., J.reine und angew.Math. 1934, Vol.171, pp.193-226). In several ways the spaces  $A_R$  and  $\bar{A}_R$  can be realized as spaces of analytic functions in

certain regions of the complex plane. If especially the function

$x(z) = \sum_{i=0}^{\infty} x_i z^i$  is adjoint to the sequence  $x(x_0, x_1, \dots)$  then  $A_R (\bar{A}_R)$  becomes

the space of analytic functions in the open (closed) circle  $|z| < R$  ( $|z| \leq R$ ),

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C111/C222

# Linear Operators in an Analytic Space

and here the introduced topology is identical with the topology generally usual in these spaces. The first chapter of the paper contains the description of such topological notions in the  $A_R$  ( $\bar{A}_R$ ) as the convergence of the sequences, simple and strengthened boundedness of the subsets, and compactness. The second chapter treats the description of linear non-limit-operators which map an analytic space into another. Basic results: Theorem 1: In order that a matrix  $[a_{jk}]$  transforms an (arbitrary) analytic space  $A$  into  $A_{R_1}$ ,  $R_2 \neq 0$ , it is necessary and sufficient that for every

$r < R_1$  the inequality  $|a_{jn}|r^j \leq c_n$  is satisfied, where  $j, n=0, 1, \dots$ , and the point  $c(c_0, c_1, \dots)$  belongs to the dual space  $A^*$ .

Theorem 2: In order that the matrix  $[a_{jk}]$  transforms the space  $\bar{A}_R$  into  $A$  it is necessary and sufficient that for all  $j, n$  and  $r < 1/R$  the inequality  $|a_{jn}|r^n \leq c_j$  is satisfied, where the point  $c(c_0, c_1, \dots)$  belongs to the

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C111/C222

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space  $A$ .

Furthermore the matrix is described which represents a linear continuous operator from the Banach space  $l_p$ ,  $1 \leq p \leq \infty$ , into the analytic space  $A_1$ .

The given results and some of the proofs are published by the author in earlier papers (Doklady Akademii nauk USSR, 1951, Vol.79, No.6, and Vol.80, No.1,2).

[Abstracter's note: The above text is a full translation of the original Soviet abstract.]

Card 3/3

KHAPLANOV, M.G.

Linear functionals in a space of single-valued analytic  
functions. Trudy Sem. po funk. anal. no. 3/4:115-121 '60.  
(MIRA 14:10)

(Functions, Analytic)



VOROVICH, I.I.; KHAPLANOV, M.G.

Work of Rostov mathematicians in recent years. Usp. mat. nauk 18  
no.2:211-233 Mr-Apr '63. (MIRA 16:8)  
(Rostov--Mathematics)

RUKHMAN, L.Ye.; RAYEVSKAYA, T.P.; KHAPMAN, V.L.

Insertion appliances of polyethylene in foot defects. Ortop.,  
travm. i protez. no. 1877-30'63. (MIRA 16:10)

1. Iz detskey kliniki (zav. - doktor med. nauk L.Ye. Rukhman)  
Leningradskogo instituta protezirovaniya (dir. - dotsent M.V.  
Strukov).

KHAPOV, V.S.; KORYAYEVA, A.I.; TEMNOV, Yu.A.

Improving the quality of stuffing box packings. Avt. i trakt. prom.  
no.12:34-36 D '57. (MIRA 11:1)

1. Yaroslavskiy avtozavod,  
(Packing (Mechanical engineering))

SOV/113-59-5-9/21

12(2)

AUTHORS: Zaytsev, K.S.; Khapov, V.S.

TITLE: Experience in Testing Automobile Transmissions on Test Stands

PERIODICAL: Avtomobil'naya promyshlennost', 1959, Nr 5, pp 24-25 (USSR)

ABSTRACT: The authors describe briefly three types of test stands used for investigating the functioning of automobile transmissions at the Yaroslavl' Engine Plant. A torsion test stand for determining the static strength of assembled transmission components is shown by photograph, Figure 1. A test stand for wear and fatigue tests of transmissions is shown by photograph, Figure 2. With this device two transmissions may be tested simultaneously, while a third one serves as a reductor. A test stand for transmission gear shift mechanisms is shown by photograph, Figure 3. Gear shifting is performed automatically by a pneumatic device at

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Experience in Testing Automobile Transmissions on Test Stands

a rate of six shifts per minute. As an example for a more complete utilization of these test stands, the authors mention the investigation of transmissions, containing parts made of different types of steel 12KhNZA, 18KhGT, 30KhGT and 15KhGNTA, whereby the best results were obtained with the latter steel. However, the proper temperature conditions must be selected when hardening parts made of steel 15 KhGNTA. It is possible to use steel-steel sliding friction bearings in YaMZ transmission, in case one of the bearing parts is parkerized. Steel and cast iron are not suitable for manufacturing tapered synchronizer rings since they have too high a wear and disturb the normal work of synchronizers. Further, the selection of the proper lubricant is of importance. There are 3 photographs.

ASSOCIATION: Yaroslavskiy motornyy zavod (Yaroslavl' Engine Plant)  
Card 2/2

71117206 89-7-9/32

AUTHORS: Dmitriyev, P.P., Krasnov, N.N., Khaprov, Ye.N. 89-7-9/32

TITLE: On the Problem of the Deflection of a Bundle in a Cyclotron  
(K voprosu ob otklonenii puchka v tsiklotrone)

PERIODICAL: Atomnaya Energiya, 1957, Vol. 3, Nr 7, pp. 45-47 (USSR)

ABSTRACT: At first some previous works dealing with this subject are discussed. The experiments for the production of a deflected bundle were carried out by means of a meter cyclotron. According to computation a deuteron energy of 10.6 MeV corresponds to the output radius of 44 cm. The magnetic field here decreases by 2.2% and the coefficient for the decrease of the magnetic field amounts to  $n = 0.2$ . A schematical section through the chamber of the cyclotron is shown by a schematical drawing. An ion source with covered-up arcs was used on the occasion of these experiments. The shifting of the source and the control of its location takes place by remote control without switching off of the cyclotron. The high voltage is transferred into the duants in form of pulses with a frequency of 200 pulses per sec. The voltage amplitude between the duants amounts to from 90 to 100 kV. The current intensity of the inner bundle amounts to from 800 to 100 micro-

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On the Problem of the Deflection of a Bundle in a Cyclotron

89-7-9/32

ampères within the pulse. The current intensity of the deflected bundle can be registered on three places by means of the targets M1, M2, and M3. Measuring takes place simultaneously by means of a thermal and an electric method. The first experiments were carried out by means of the usual deflector with plane electrodes. With the shifting of the ion source a sharp maximum in the current intensity of the deflected bundle is observed. With the modification of the amplitude of the voltages between the duants a new location of the source had to be chosen for the purpose of obtaining the maximum current intensity. (Numerical data are given). It was possible to increase the current intensity of the deflected bundle (on the target M1) up to from 45-50% of the current intensity of the interior bundle. Next, a deflecting system with hyperbolic electrodes was investigated. The current intensities registered on all three exterior targets were equal to one another, which signifies a shortening of the horizontal dimensions of the bundle. There are 3 figures and 6 references, 4 of which are Slavic.

SUBMITTED: February 8, 1957

AVAILABLE: Library of Congress

Card 2/2

1. Ion bundles - Deflection - Test results
2. Cyclotrons - Operation

КНАПРОУ, Ye. N.

PHASE I BOOK EXPLOITATION NOV/1997

Vsesoyuznaya nauchno-tekhnicheskaya konferentsiya po primeneniyu radioaktivnykh i stabil'nykh izotopov i izlucheniya v narodnom khozyaystve i nauke, Moscow, 1957

Polucheniye izotopov. Moshchnyye gamma-izotopnyye radioisotopy i dosimetriya; trudy konferentsii... (Isotope Production. High-energy Gamma-Radiation Facilities. Radiometry and Dosimetry; Transactions of the All-Union Conference on the Use of Radioactive and Stable Isotopes and Radiation in the National Economy and Science) Moscow, Izdatel'stvo AN SSSR, 1958. 293 p. 5,000 copies printed.

Sponsoring Agency: Akademiya nauk SSSR; Glavnoye upravleniye po ispol'szovaniyu atomnoy energii SSSR.

Editorial Board: Frolov, Yu.S. (Resp. Ed.), Zhavoronkov, N.N. (Deputy Resp. Ed.), Aglintsev, I.K., Alekseyev, B.A., Bockharov, V.V., Isakhsinskiy, M.I., Malov, T.P., Sinityn, V.I., and Pepova, G.I. (Secretary); Tech. Ed.: Morichov, M.D.

REMARKS: This collection is published for scientists, technologists, persons engaged in medicine or medical research, and others concerned with the production and/or use of radioactive and stable isotopes and radiation.

COVERAGE: Thirty-eight reports are included in this collection under three main subject divisions: 1) production of isotopes 2) high-energy gamma-radiation facilities, and 3) radiometry and dosimetry.

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PART I. PRODUCTION OF ISOTOPES

Frolov, Yu.S., V.V. Bockharov, and Ye.Ye. Kulish. Development of Isotope Production in the Soviet Union. This report is a general survey of production methods, apparatus, raw materials, applications, investigations, and future prospects for radio isotopes in the Soviet Union.

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*Khaprov, Ye. N.*

21(8)

AUTHORS:

Guldamashvili, A. I., Dmitriyev, P. P. SOV/89-5-6- 18/25  
Krasnov, N. N., Mishin, V. Ya.,  
Khaprov, Ye. N.

TITLE:

The Production of the Isotope  $As^{74}$  by Means of a Cyclotron  
(Polucheniye izotopa  $As^{74}$  na tsiklotrone)

PERIODICAL:

Atomnaya energiya, 1958, Vol 5, Nr 6, pp 660 - 661 (USSR)

ABSTRACT:

$As^{74}$  was obtained by the irradiation of metallic germanium with the external 10,8 MeV deuteron beam of the cyclotron (Ref 5).  
The characteristic feature of the target was the fact that the cooling water immediately reached the inner surface of the irradiated germanium plate. The germanium plate was cast in a vacuum and was then ground to the dimensions 170.40.4 mm<sup>3</sup>. The deuteron beam (60-70  $\mu$ A) is limited by a shutter so that only a surface of 150.25 mm<sup>2</sup> of the germanium was irradiated. The water consumption was 5 l/m.  
Chemical separation was carried out as follows: After the irradiated sample had been boiled twice (for 15 to 20 minutes) in aqua regis, about 97-98 % of the activity had dissolved.

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The Production of the Isotope  $\text{As}^{74}$  by Means of  
a Cyclotron

SOV/89-5-6-18/25

The solution was steamed-in and extracted with 11 n HCl (method according to reference 6). The arsenic carrier used weighed 50  $\mu\text{g}$ . Concentration of the arsenic isotope was carried out by the Marsh method (arsenic hydride). The two preparations, which were enclosed in an ampoule of 0,6  $\text{cm}^3$ , had an initial activity of 60 mCi. The  $\text{As}^{74}$  activity was measured by comparison with a  $\text{Co}^{60}$  source by means of the micro-roentgenometer of the type "Kaktus" 30 days after irradiation. The total yield obtained by the formation of  $\text{As}^{74}$  was:

25  $\mu\text{Ci}/\mu\text{A.h} \pm 15\%$ . The half time was:  $T_{1/2} = 18,4 \pm 0,4$  d.

Professor B. S. Dzhelepov, I. P. Selinov, and Ye. Ye. Baroni interested themselves in this work. M. Z. Maksimov calculated the yield curve. Yu. A. Bliodze and I. I. Zhivotovskiy assisted in carrying out experiments. There are 2 figures and 10 references, 3 of which are Soviet.

Card 2/3

KHARA, I S

Khara, I. S. On a method of approximate conformal mapping of a many cornered region onto the unit circle; Dopovid Akad. Nauk Ukrain. RSR 1953, 281-293. (Ukrainian. Russian summary)

A numerical method for approximating the constants which occur in the application of the Christoffel-Schwarz method for the conformal representation of polygonal regions is given with examples. C. Salzer.

*Khar'kov Polytech. Inst. in V.I. Lenin*

KHARA, I.S.; SAVIN, G.M., diisnyi chlen Akademiyi nauk URSR.

Investigation of stress concentration during dilation in infinite plates weakened by arched or trapezoid apertures. Dop.AN URSR no.4:294-298 '53.  
(MLBA 6:8)

1. Kharkivs'kyi politekhnichnyi instytut imeni V.I.Lenina. 2. Akademiya nauk URSR (for Savin).  
(Elastic plates and shells)

KHARA, I.S.; SAVIN, G.M., diisnyi chlen Akademiyi nauk URSR.

Investigation of stress concentration in thick plates beside arched and trapezoid apertures supported by absolutely rigid rings. Dop.AN URSR no.4: 299-303 '53. (MLRA 6:8)

1. Kharkivs'kyi politekhnichnyi instytut imeni V.I.Lenina. 2. Akademiya nauk URSR (for Savin). (Elastic plates and shells)

16(1)

AUTHOR: Khara, I.S.

SOV/20-126-6-15/67

TITLE: Some Approximate Formulas in the Theory of Conformal Mappings

PERIODICAL: Doklady Akademii nauk SSSR, 1959, Vol 126, Nr 6,  
pp 1210-1213 (USSR)

ABSTRACT: The conformal mapping of the unit circle  $|z| < 1$  onto an arbitrary closed polygon of the  $\zeta$ -plane is carried out by the Christoffel - Schwarz integral as is well-known. For three classes of polygons (which differ strongly from the circle) the author gives approximative formulas in which the sides of the polygons are explicitly expressed by the Christoffel-Schwarz constants. Let the polygon be e.g. a rectangle with the angles  $A_1, A_2, A_3, A_4$ , where the point  $\zeta = 1$  is assumed to lie in the center of  $A_1 A_2$ . Let the constants  $-\varphi, \varphi, \pi - \varphi, \pi + \varphi$  correspond to the angles. If it is  $\overline{A_2 A_3} : \overline{A_1 A_2} = \lambda \gg 1$  (extended rectangle), then it holds

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Some Approximate Formulas in the Theory of  
Conformal Mappings

SOV/20-126-6-15/67

approximately  $A_1 A_2 = \frac{\pi}{2}$  ,  $A_2 A_3 = \ln \frac{4}{\varphi}$  ,  $\varphi = 4 e^{-\frac{\pi \Delta}{2}}$  .

The author gives similar formulas in the two other more complicated cases. Since the lateral lengths are expressed by

integrals of the type  $\int_{\varphi_{k-1}}^{\varphi_k} |f(\zeta)| |d\zeta|$ , the approximation

formulas are obtained by approximative calculation of these integrals.

There are 3 figures.

ASSOCIATION: Khar'kovskiy politekhnicheskii institut imeni V.I. Lenina  
(Khar'kov Polytechnical Institute imeni V.I. Lenin)

PRESENTED: March 12, 1959, by S.L. Sobolev, Academician

SUBMITTED: March 9, 1959

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30713

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S/020/61/141/003/005/021  
C111/C444

AUTHOR: Khara, I. S.

TITLE: A numerical method of solving eigenvalue problems

PERIODICAL: Akademiya nauk SSSR. Doklady, v. 141, no. 3, 1961,  
574 - 577

TEXT: Let  $s$  in the characteristic equation

$$1 + a_1 \lambda + a_2 \lambda^2 + \dots + a_s \lambda^s = 0 \quad (1)$$

of a one-dimensional boundary value problem be such that the first  $s_0$  eigenvalues can be determined with an error not higher than some per cents. In the determination of the eigenvalues of the boundary value problems for

$$q_1(x)y'(x) + q_2(x)y''(x) + \dots + q_n(x)y^{(n)}(x) - \lambda r(x)y(x) \quad (2)$$

where the coefficients are smooth, the homogeneous system of equations for  $y_k^{(1)} = y^{(1)}(\frac{k-1}{s})$  ( $k = 1, 2, \dots, s+1$ ) be obtained by multiple integration. The following integrals are obtained:

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A numerical method of solving...

$$\int_{x_{\omega}}^{x_{\omega+k}} \int_{x_{\omega}}^x \dots \int_{x_{\omega}}^x r(x)y(x)dx^v \quad (3)$$

In order to replace those by finite sums, the following formulas

$$\int_0^{x_k} \int_0^x \dots \int_0^x \varphi(x) \psi(x) dx^v = b^v \sum_{i=1}^m A_{ki}^{(v,m)} [\varphi] \psi(x_i) + R_k^{(v,m)}; \quad (4)$$

$$\int_0^{x_k} \int_0^x \dots \int_0^x \psi(x) dx^v = \frac{b}{(v-1)!} \sum_{i=1}^m A_{ki}^{(1,m)} [1] (x_k - x_i)^{v-1} \psi(x_i) + \bar{R}_k^{(v,m)}; \quad (5)$$

$$A_{ki}^{(v,m)} [\varphi] = \sum_{j=1}^p B_{ki,j}^{(v,m,p)} \varphi(x_j), \quad x_i = \frac{i-1}{p-1} b, \quad x_j = \frac{j-1}{m-1} b, \quad (6)$$

$$B_{ki,j}^{(v,m,p)} = b^{-v} \int_0^{x_k} \int_0^x \dots \int_0^x l_j^{(p)}(x) l_i^{(m)}(x) dx^v, \quad k=2,3,\dots,m,$$

are introduced, where  $l_j^{(p)}(x)$  and  $l_i^{(m)}(x)$  are the coefficients of the Lagrange polynomial for the knots  $x_j$  and  $x_i$ . The special case

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A numerical method of solving...

of (4) for  $\varphi(x) = 1$  is indicated with (4a). After a comparison of the formulas (4), (5), (4a) it is recommended:

If  $r(x) = x^r$  ( $r = 0, 1, 2$ ), then in (4)  $\varphi(x) = x^r$ ,  $\psi(x) = y(x)$  is substituted, and the integrals (3) are calculated by aid of the coefficients  $A_{k,1}^{(r,m)}[x^r]$ . But if  $r(x) \neq x^r$  is slowly variable, then (3) is calculated according to the formula (4a) with  $\psi(x) = r(x)y(x)$ .

If  $r(x) \neq x^r$ , being sufficiently quick variable, then (4) is used, where  $r(x) = \varphi(x)$ ,  $\psi(x) = y(x)$  and  $A_{k,1}^{(r,m)}[\varphi]$  are determined out of (6) with  $\varphi(x) = r(x)$ .

For (2) with  $n = 2$  the boundary conditions  $y'(0) = y(1) = 0$  be given and (1) shall be constructed for a sufficiently large  $s$ . (2) is twice integrated from  $x_k$  to  $x$ , the integrals are replaced for  $x = x_{k+1}$

and  $x = x_{k+2}$  by finite sums according to (4), and two equations are obtained; after elimination of  $y'_k$  the following relation is obtained:

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A numerical method of solving...

$$y_{k+2}^{(2)} = y_{k+1}^{(1)} + y_k^{(0)}. \quad (7)$$

(7) is completed by one of the two mentioned equations with  $k = 1$ , and a homogeneous equations with  $s$  unknown quantities. By means of three examples it is shown that the recommended method is partly far more exact than e. g. the ordinary difference method. At last one considers shortly the bending oscillations of bars which are loaded by single forces.

There are 3 Soviet-bloc and 1 non-Soviet-bloc references.

ASSOCIATION: Khar'kovskiy politekhnicheskii institut im V. I. Le-  
nina (Khar'kov Polytechnical Institute im. V.I. Lenin)

PRESENTED: July 1, 1961, by I. G. Petrovskiy, Academician

SUBMITTED: June 28, 1961

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16.450

32301  
S/020/61/141/004/005/019  
C111/C222

AUTHOR: Khara, I.S.

TITLE: A method for the construction of Hermite's interpolation formula and quadrature formulas for solving boundary value problems and integral equations

PERIODICAL: Akademiya nauk SSSR. Doklady, v. 141, no. 4, 1961, 822-825

TEXT: At first it is shown that the Hermitean formula with multiple knots can be obtained by a limiting passage from the interpolation formula of Lagrange

$$f(x) = \sum_{k=1}^n l_k^{(n)}(x) f(x_k) + R(x) = \sum_{k=1}^n L_k^{(n)}(x) + R(x) \quad (1)$$

by putting  $\left[ \prod_{k=1}^n (x-x_k) \right] ; \left[ (x-x_i) (x-x_{i+1}) \right] = \omega_i(x) ; x_{i+1} = x_i + h$

and letting  $h \rightarrow 0$ .

Then the Hermitean formula is written for the interval  $[-b, b]$ ;

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X